

# Week 5 Video 5

Relationship Mining  
Network Analysis

# Today's Class

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- Network Analysis

# Network Analysis

- Analysis of anything that can be seen as connections between nodes
- Most common – social networks
  - ▣ Connections between friends on the internet
  - ▣ Connections between students in a class
  - ▣ Connections between collaborators in a work project

# Network Analysis

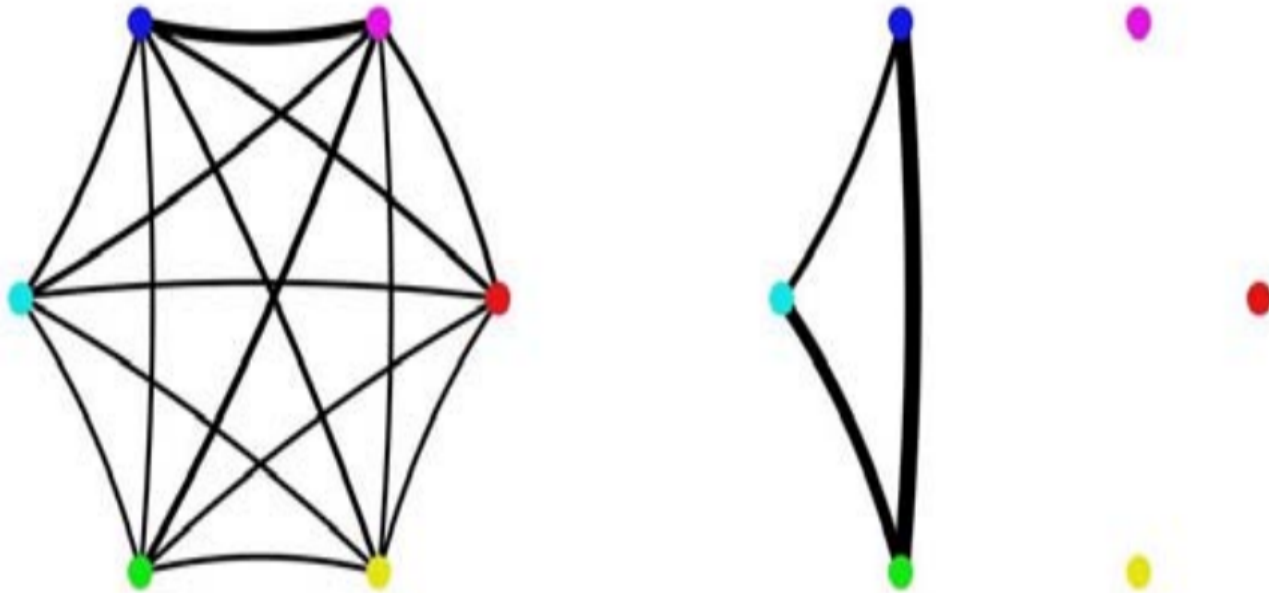
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- Could also be considered structure discovery
- Placed here in the course because of how it's typically used in practice

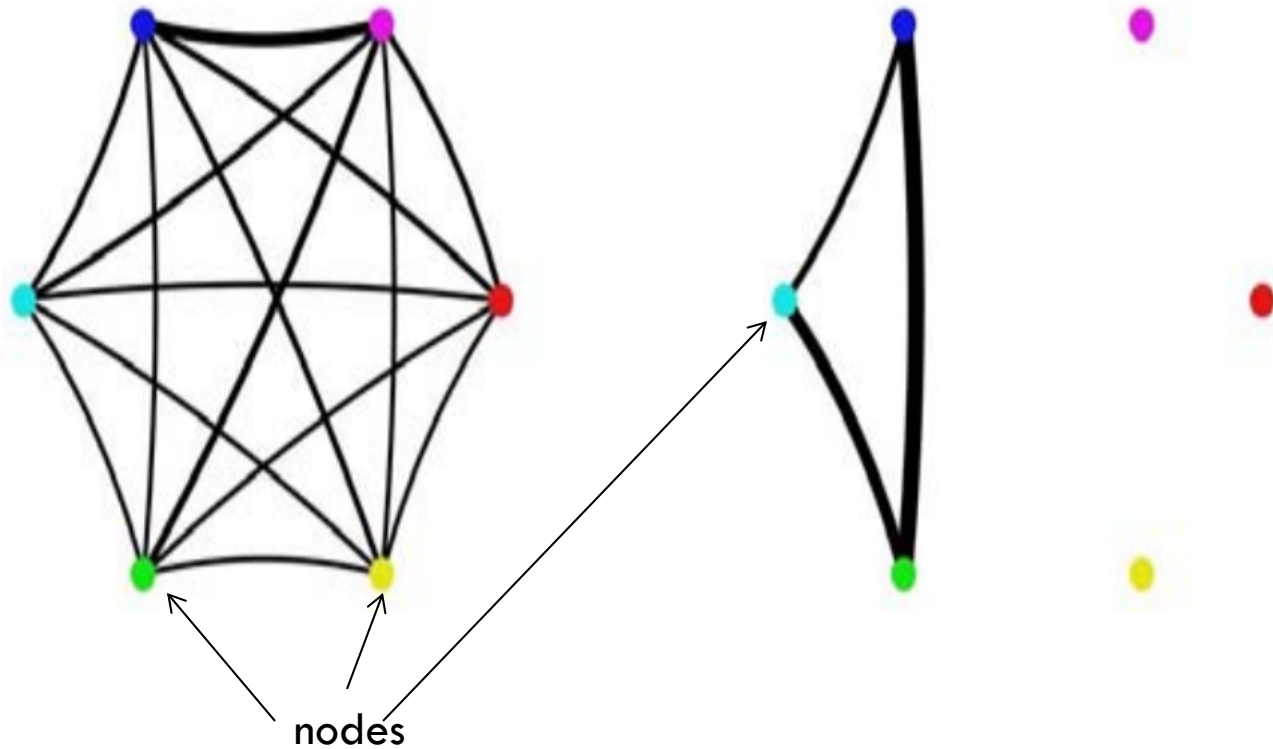
# General Postulates of Network Analysis

- There are things, referred to as nodes or vertices
- Nodes have connections to other nodes, referred to as ties or links
- Nodes can have different types or identities
- Links can have different types or identities
- Links can have different strengths

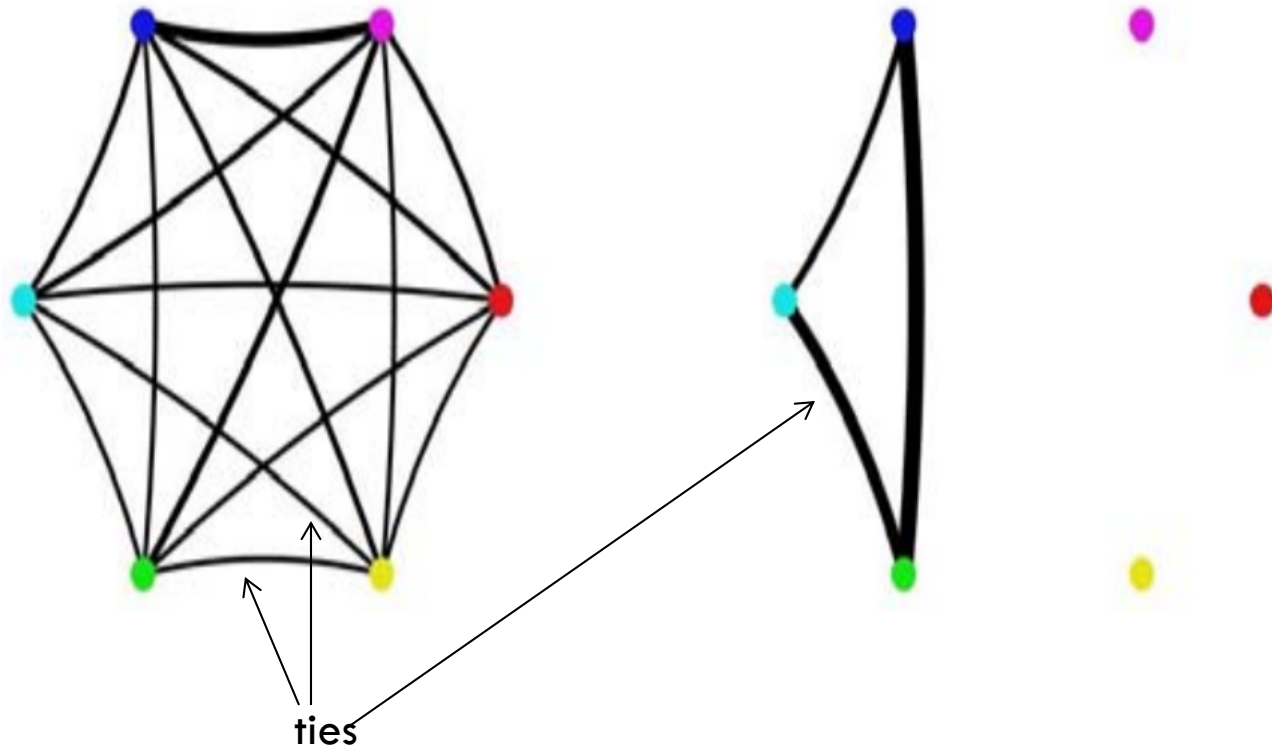
# Example: (Student work groups – Kay et al., 2006)



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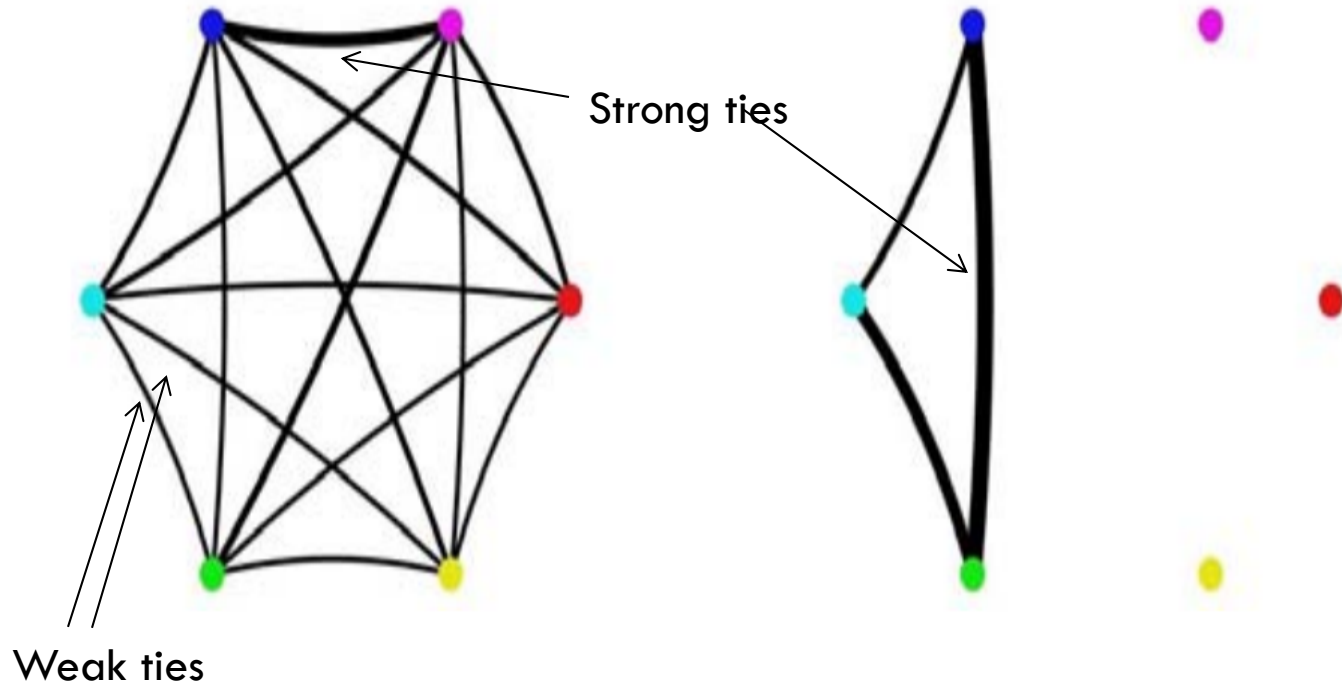


# Example: (Student work groups – Kay et al., 2006)

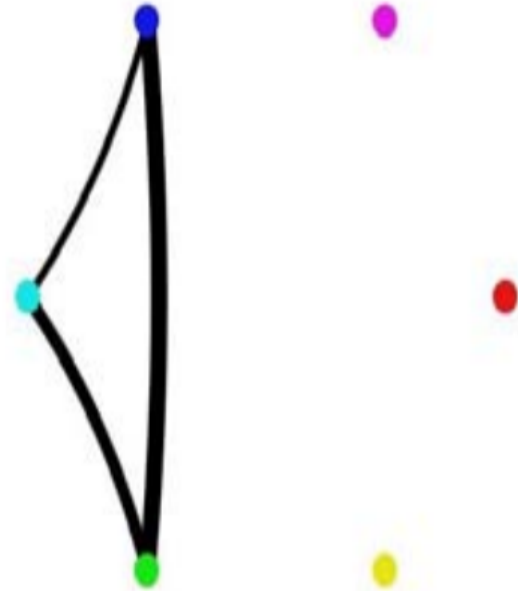
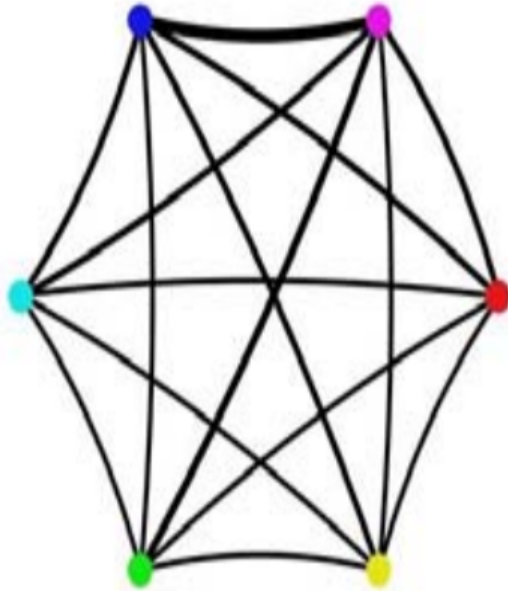




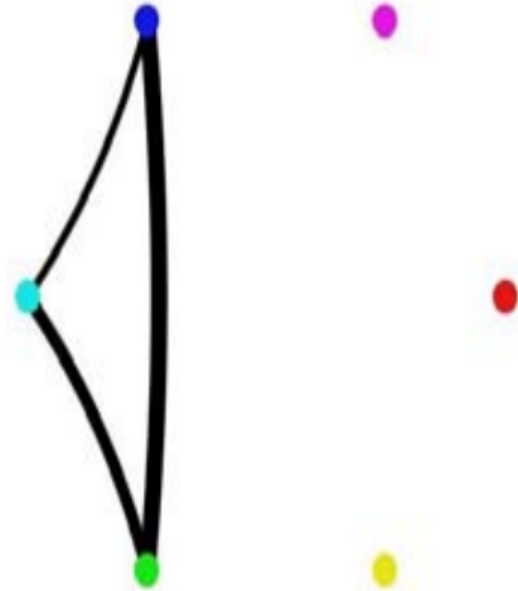
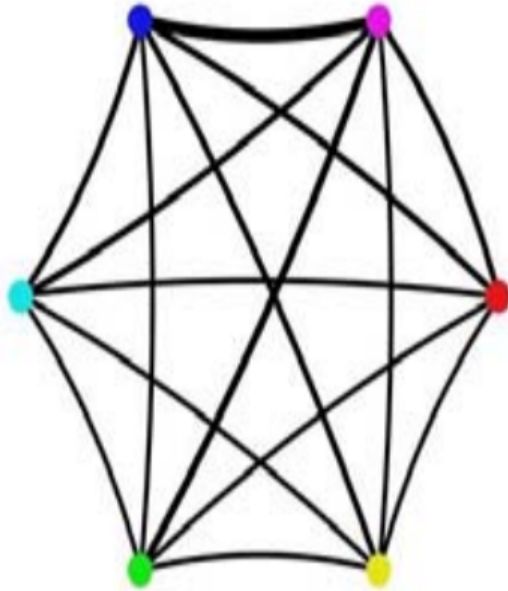
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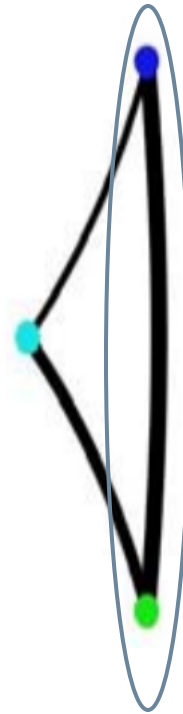
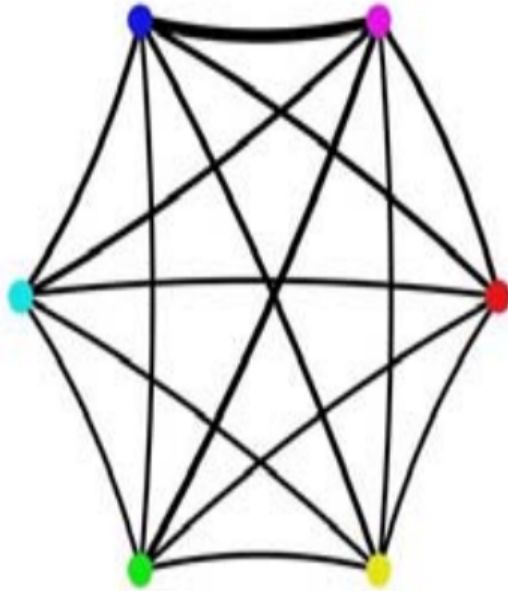
# Which student group works together better?



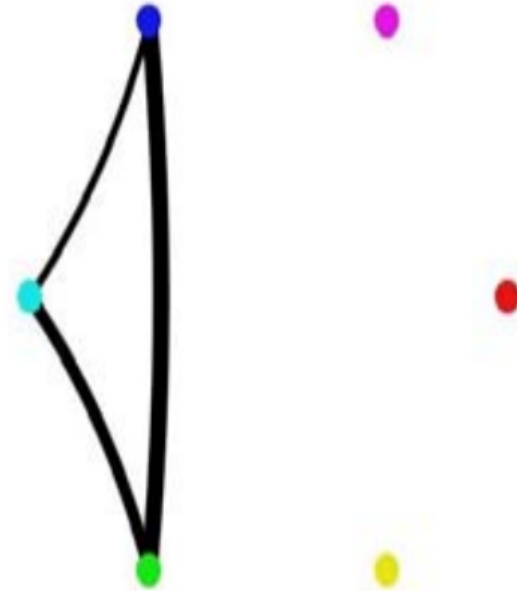
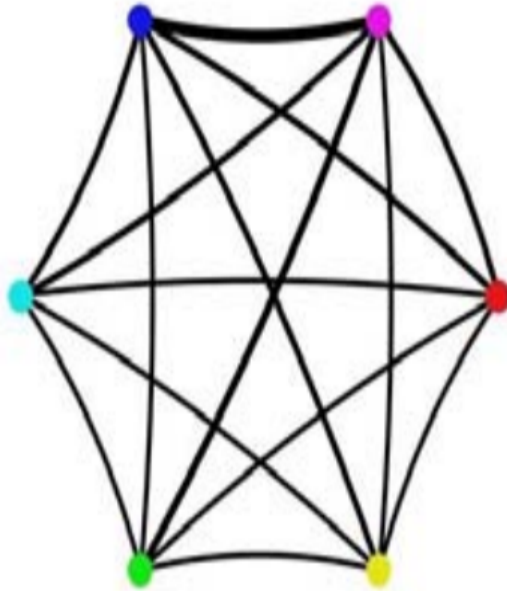
# Which is the most collaborative pair?



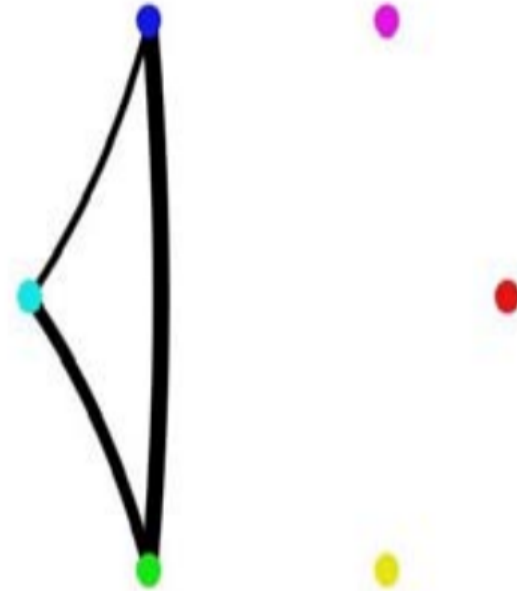
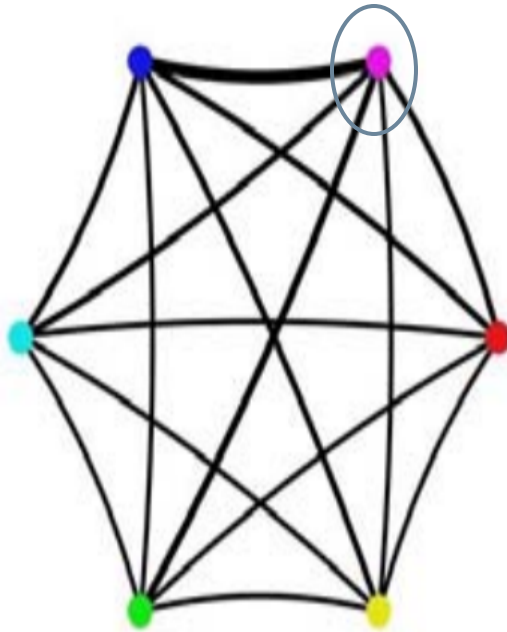
# Which is the most collaborative pair?



# Who is the most collaborative student?



# Who is the most collaborative student?



# Types

- In a graph of classroom interactions, there could be several different types of nodes
  - Teacher
  - TA
  - Student
  - Project Leader
  - Project Scribe

# Types

- In a graph of classroom interactions, there could be several types of links
  - Leadership role (X leads Y)
  - Working on same learning resource
  - Helping act
  - Criticism act
  - Insult
  
- Note that links can be directed or undirected



# Strength

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- In a graph of classroom interactions, links could be stronger or weaker due to
  - ▣ Intensity of act
  - ▣ Frequency of act

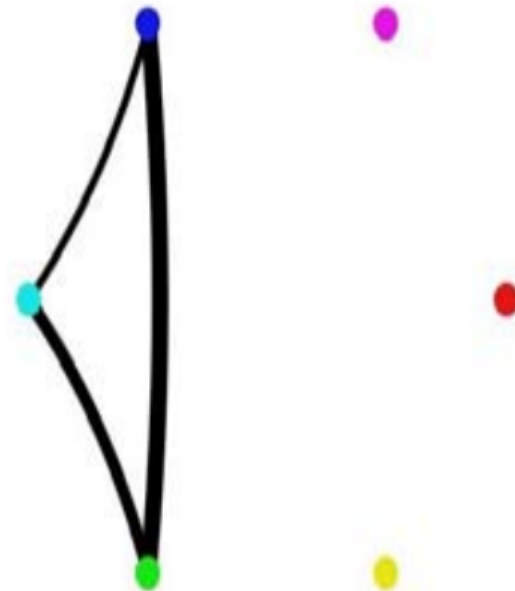
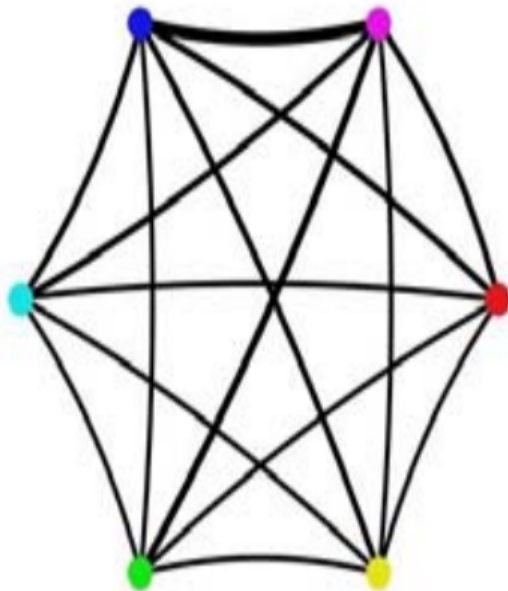
# Network Analysis

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- Use network graphs to study the patterns and regularities of the relationships between the nodes

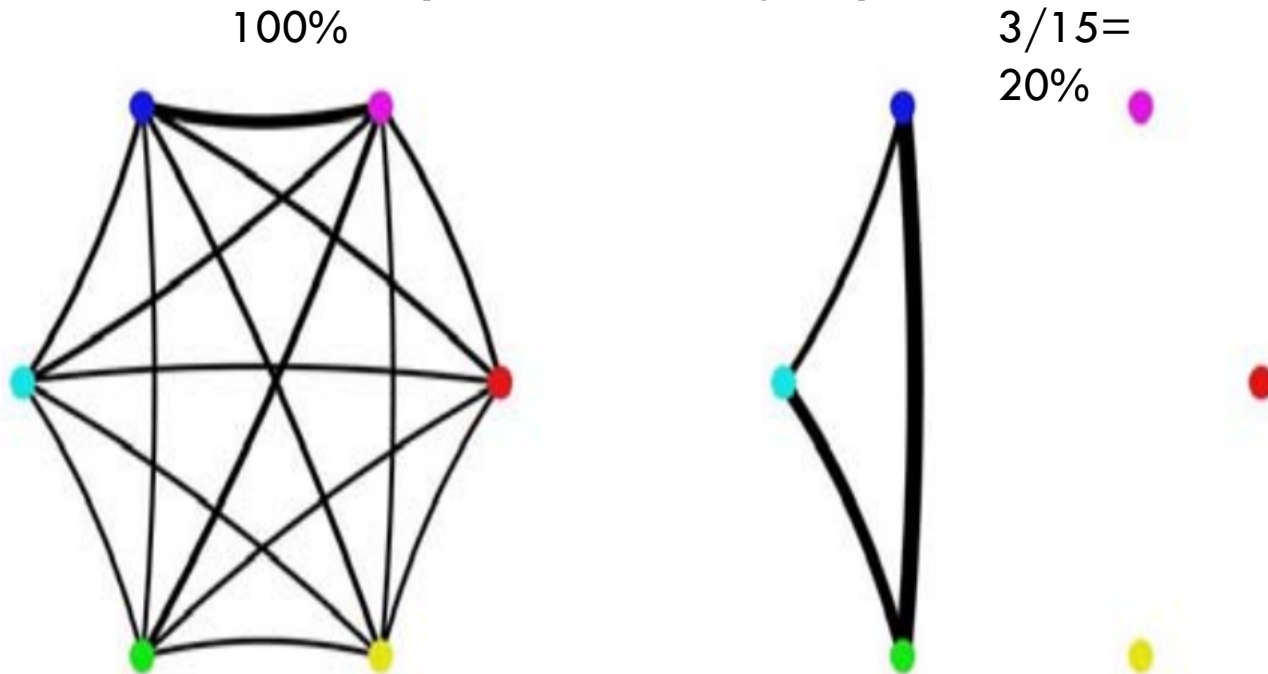
# Density

- Proportion of possible lines that are actually present in graph
- What is the density of these graphs?



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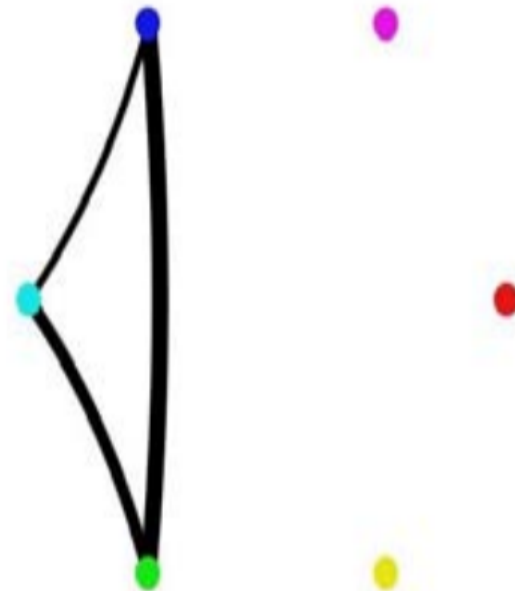
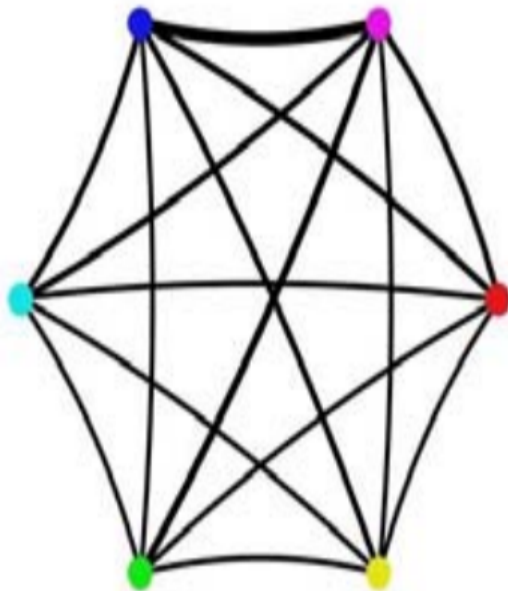
# Density

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- Could be used to figure out how collaborative a class is overall

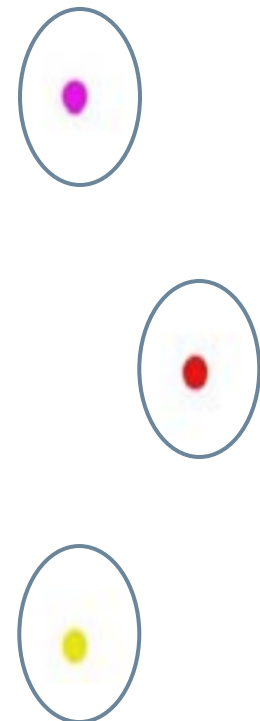
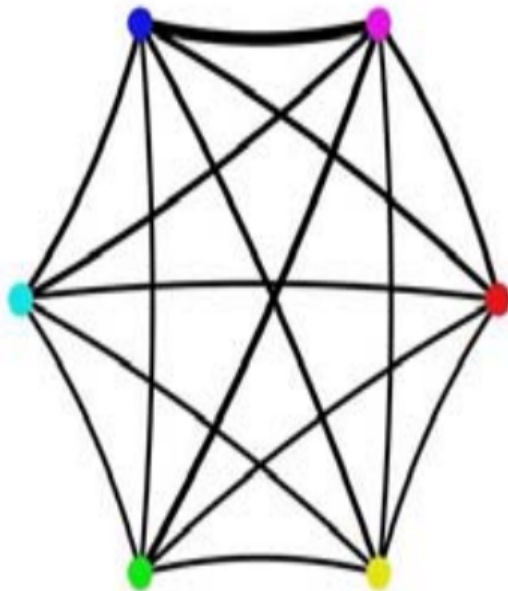
# Reachability

- A node is “reachable” if a path goes from any other node to it
- Which nodes are unreachable?



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# Reachability

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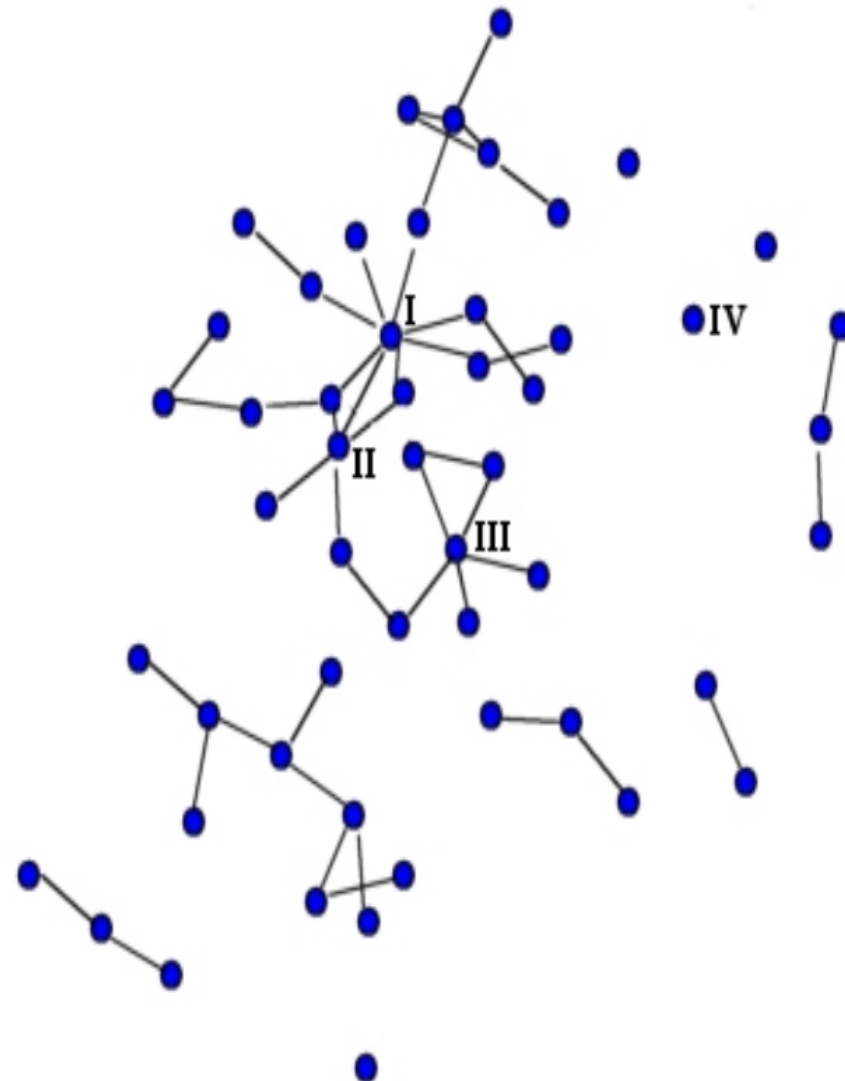
- Are there any students who don't collaborate with anybody?



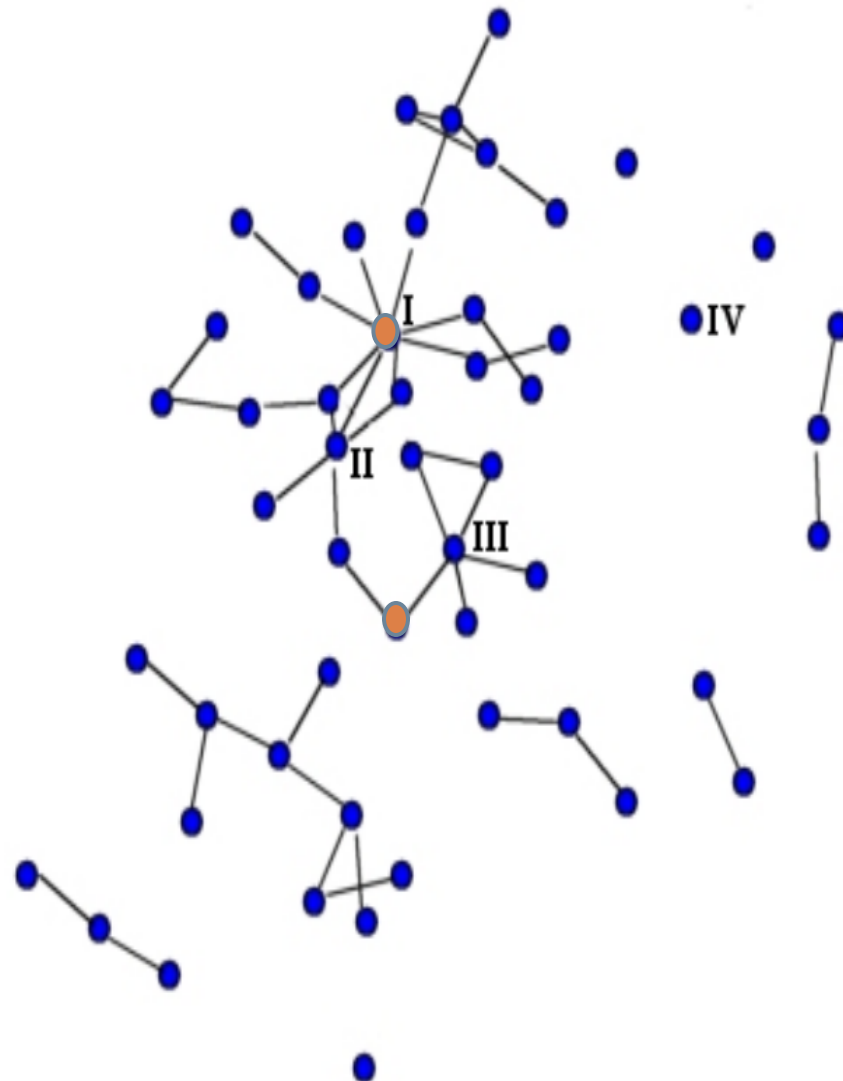
# Geodesic Distance

- The number of edges between one node  $N$  and another node  $M$ , in the shortest path connecting them

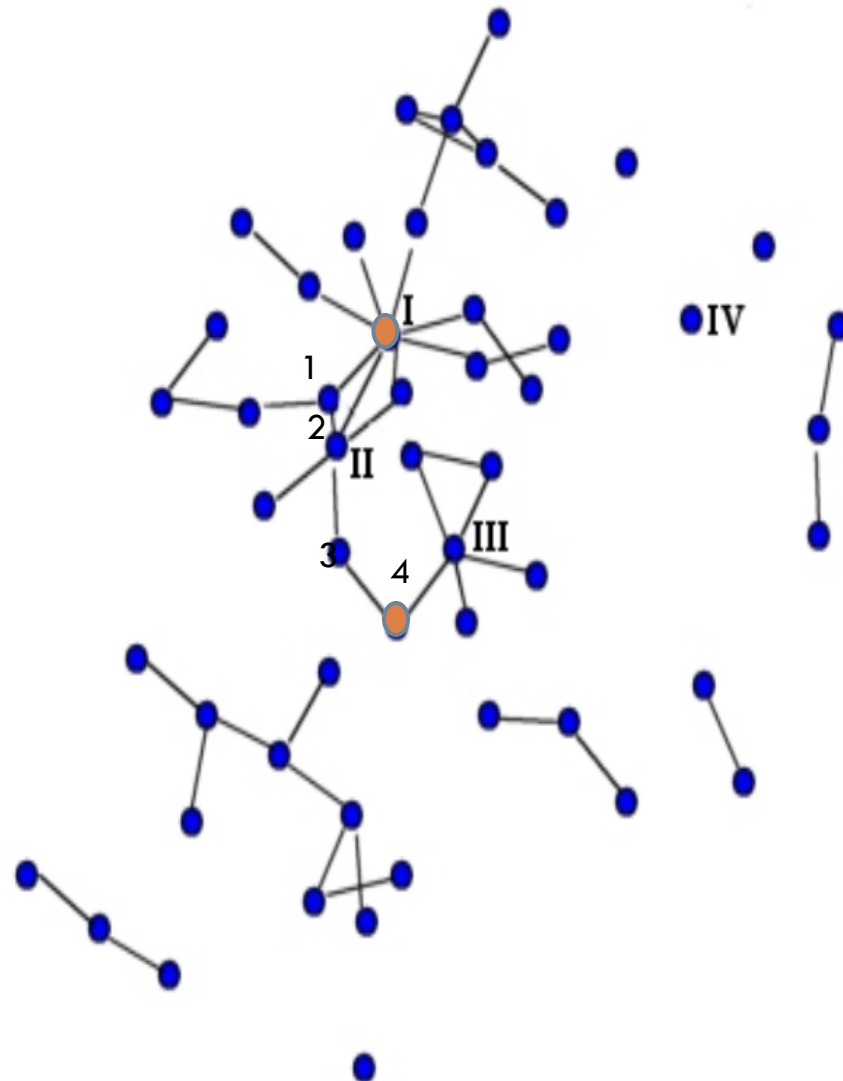
# Student social network: (Dawson, 2008)



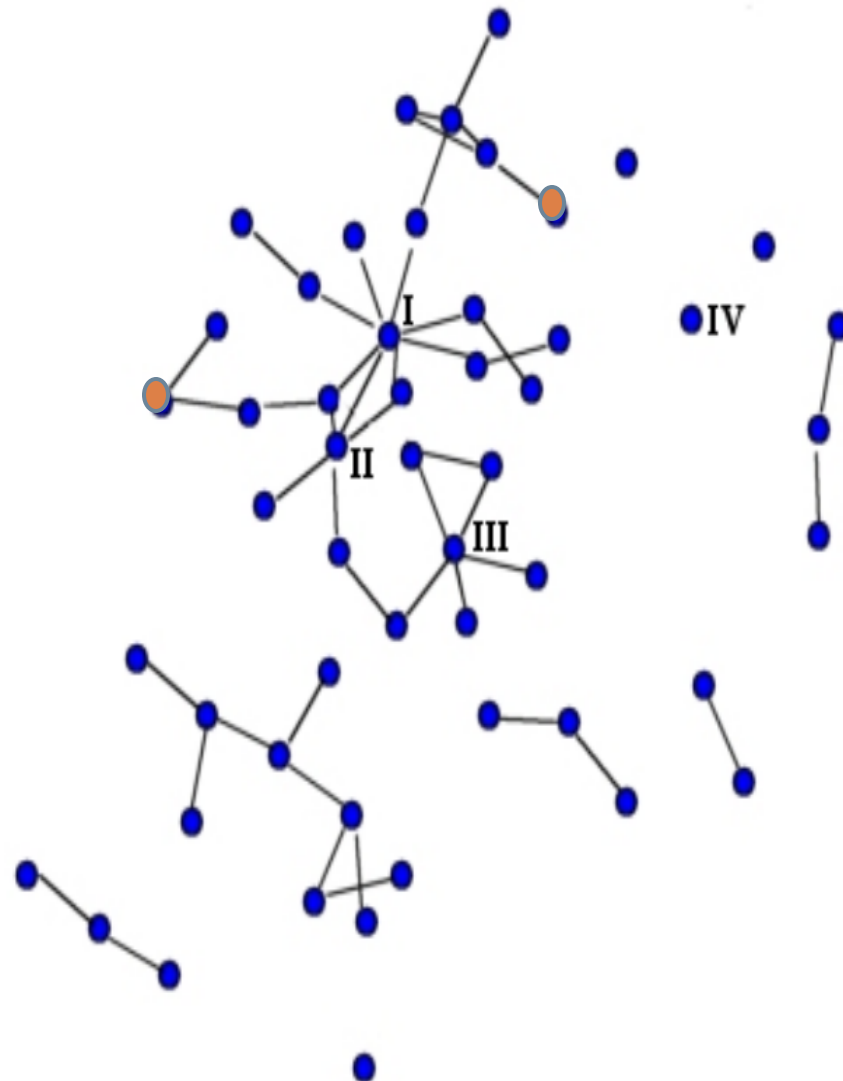
# What is the geodesic distance?



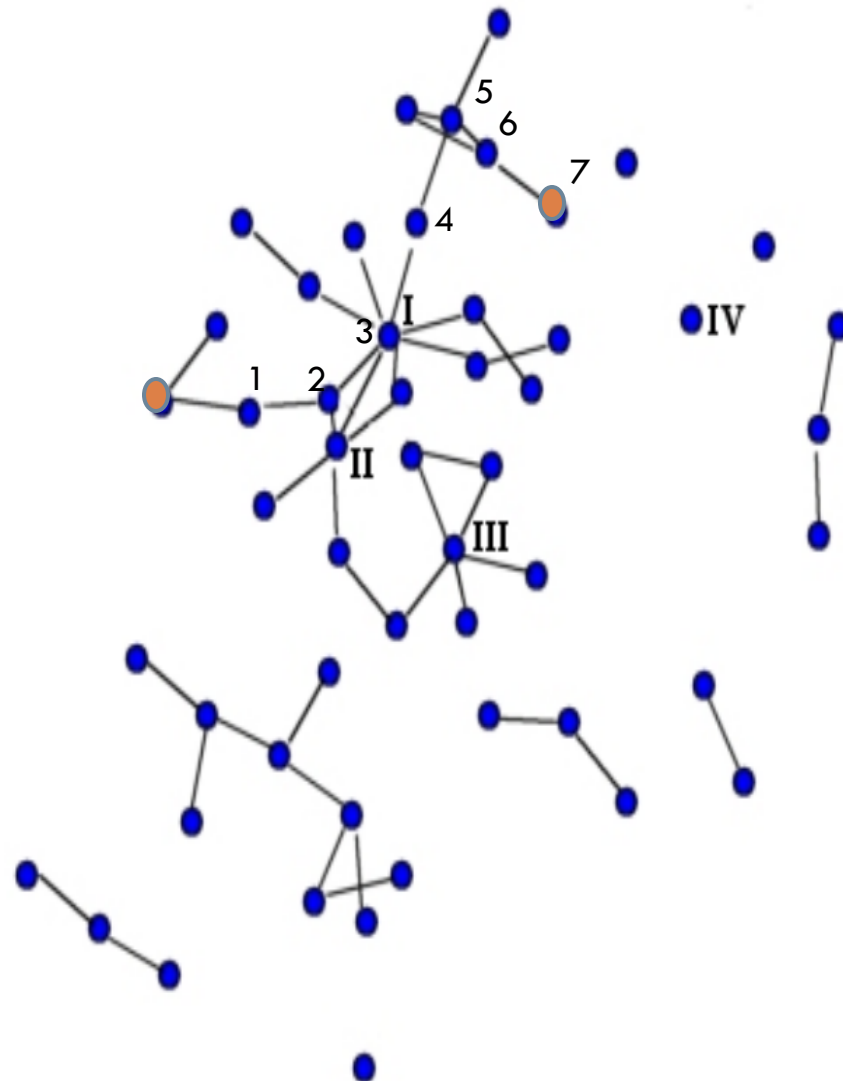
# Geodesic distance = 4



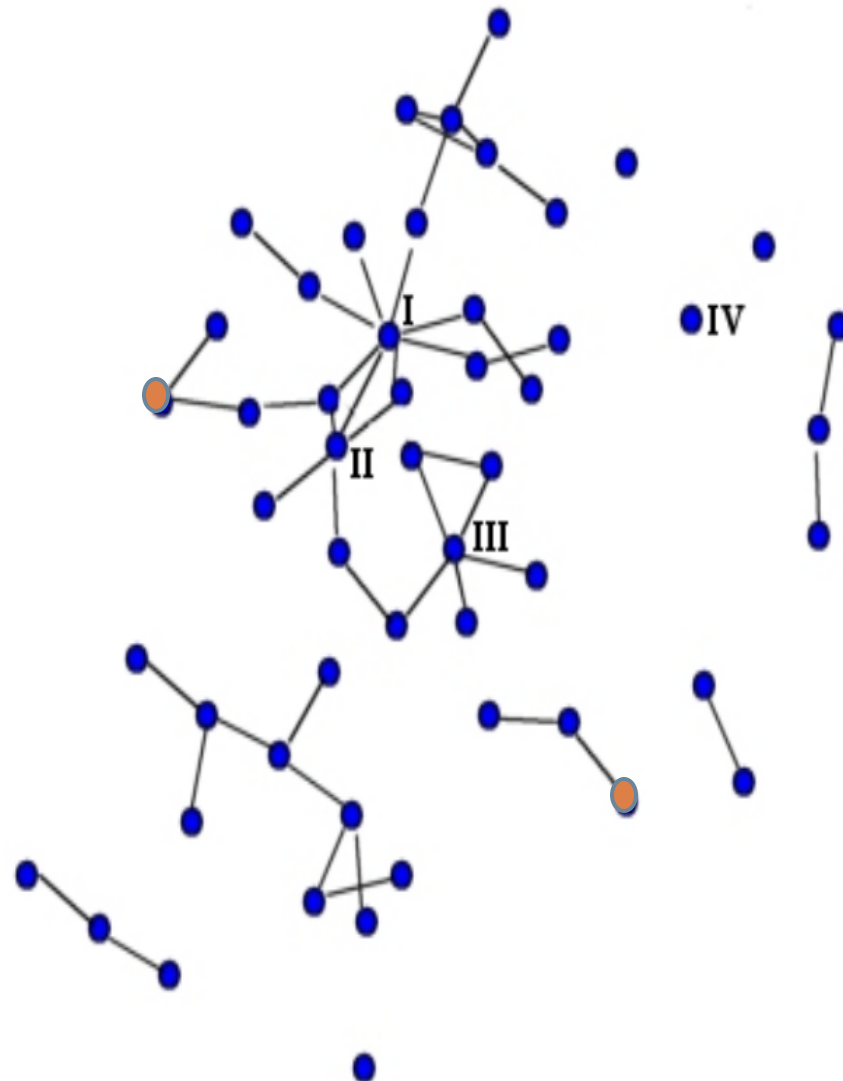
# What is the geodesic distance?



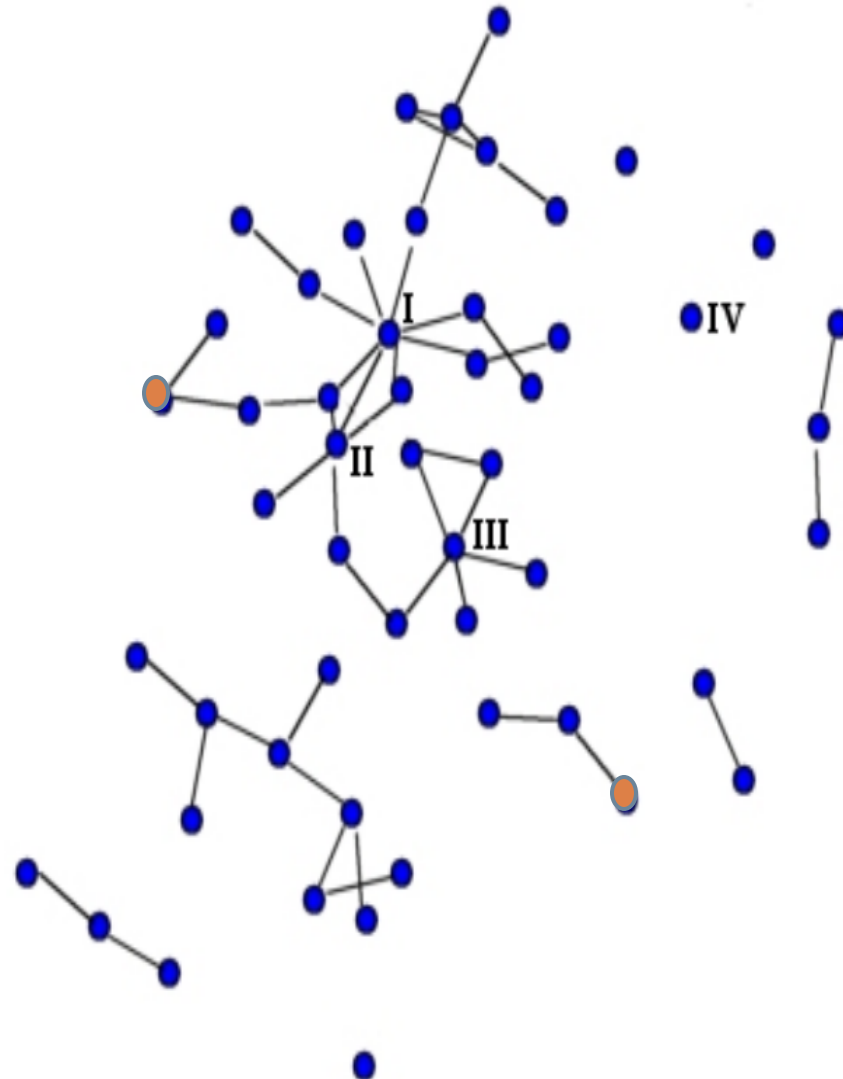
# Geodesic Distance = 7



# What is the geodesic distance?



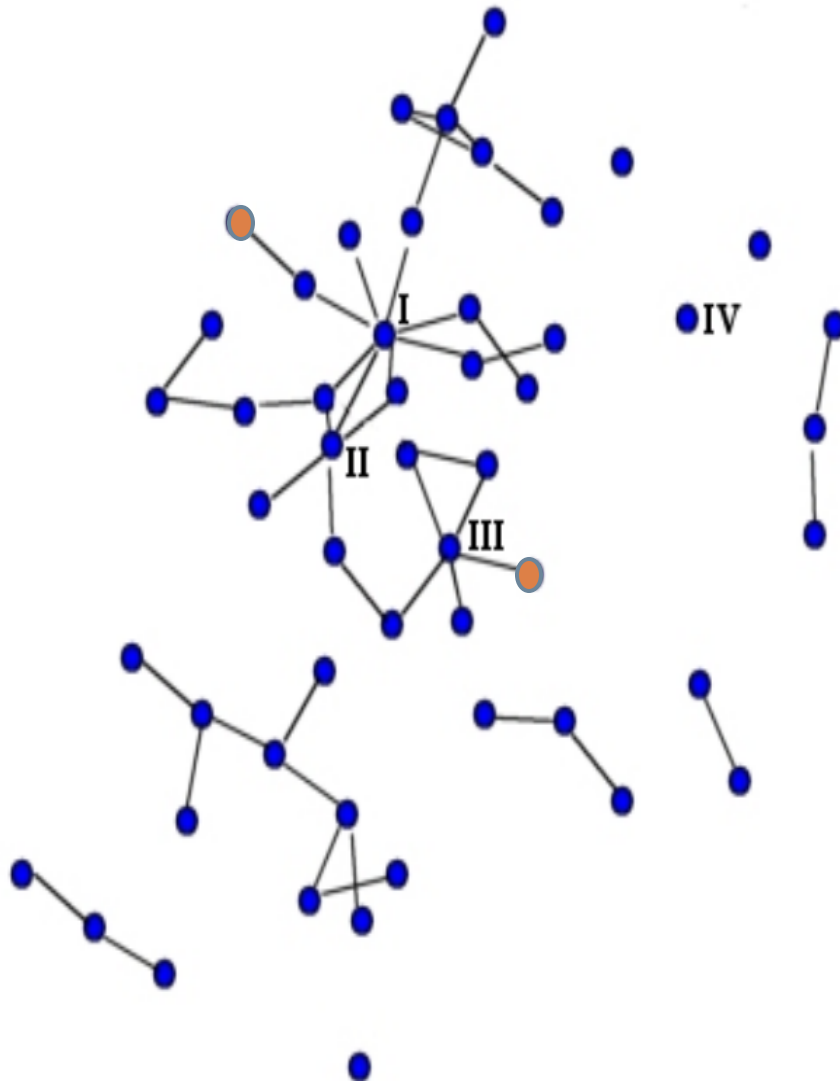
# Geodesic Distance = Infinite





# Quiz

## What is the geodesic distance?



- A) 6
- B) 7
- C) 8
- D) 9

# Geodesic Distance

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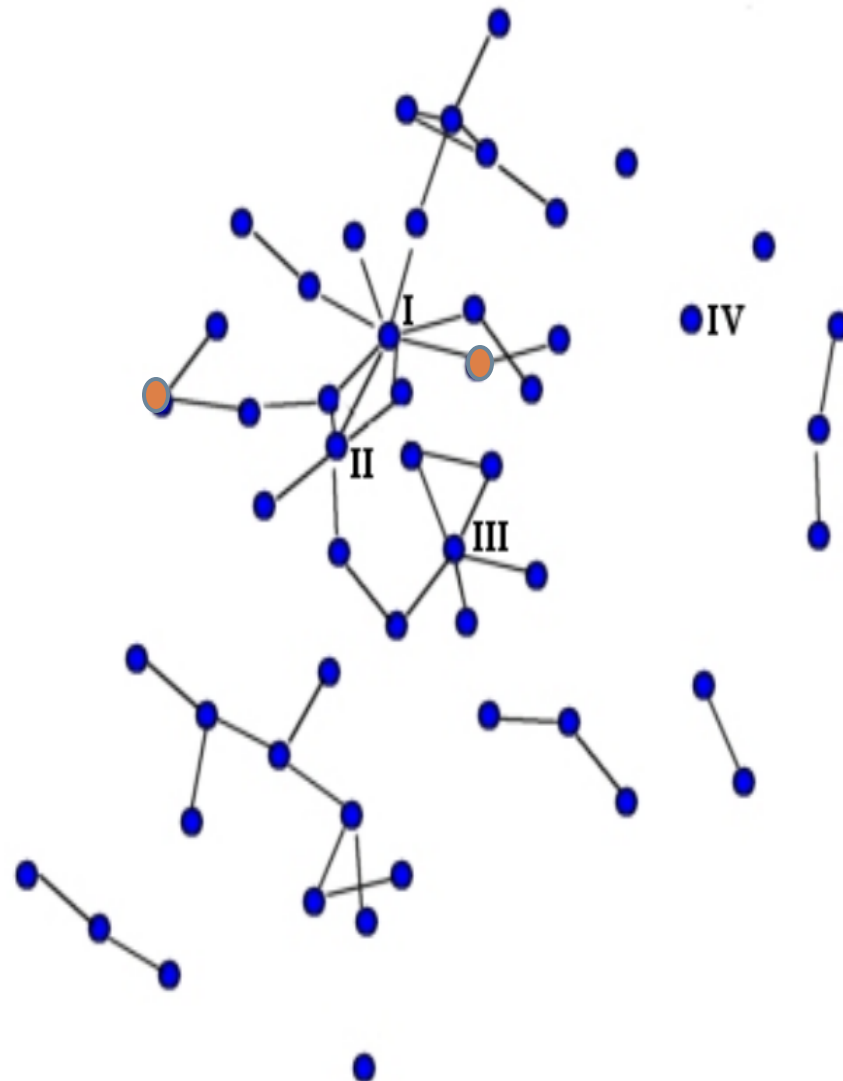
- How many people does an idea need to go through to get between people?

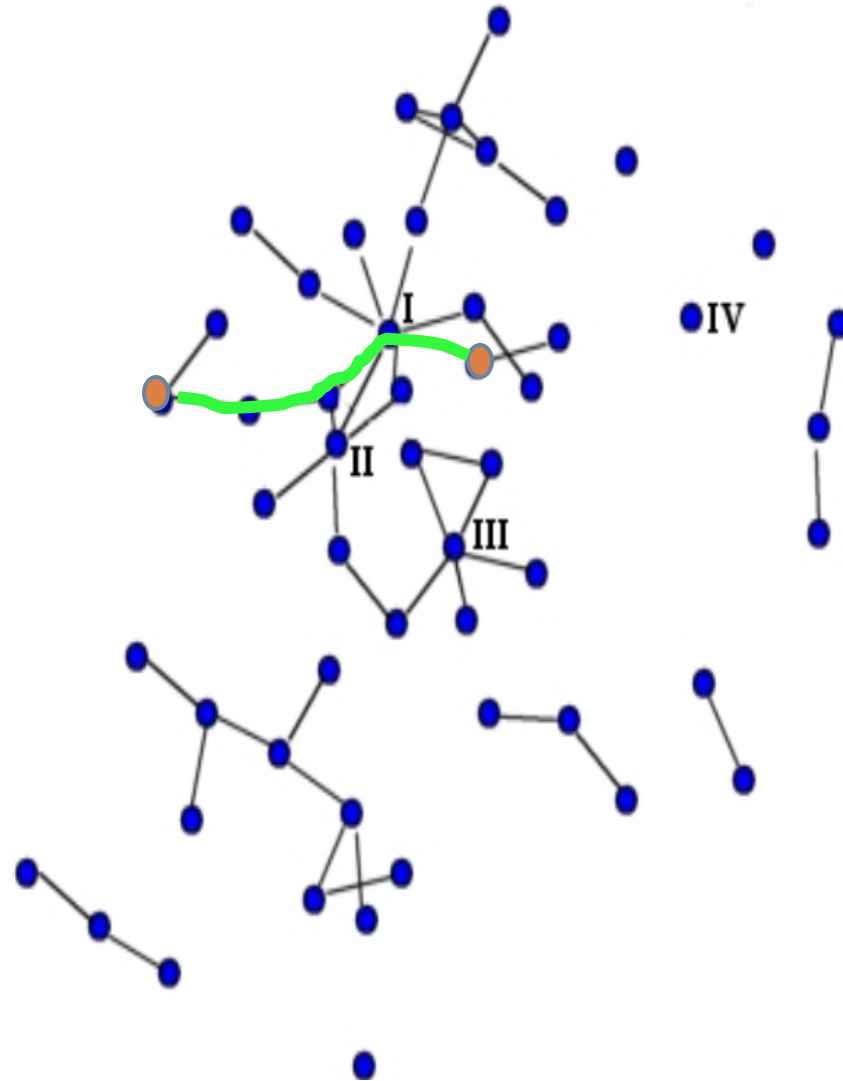
# Flow

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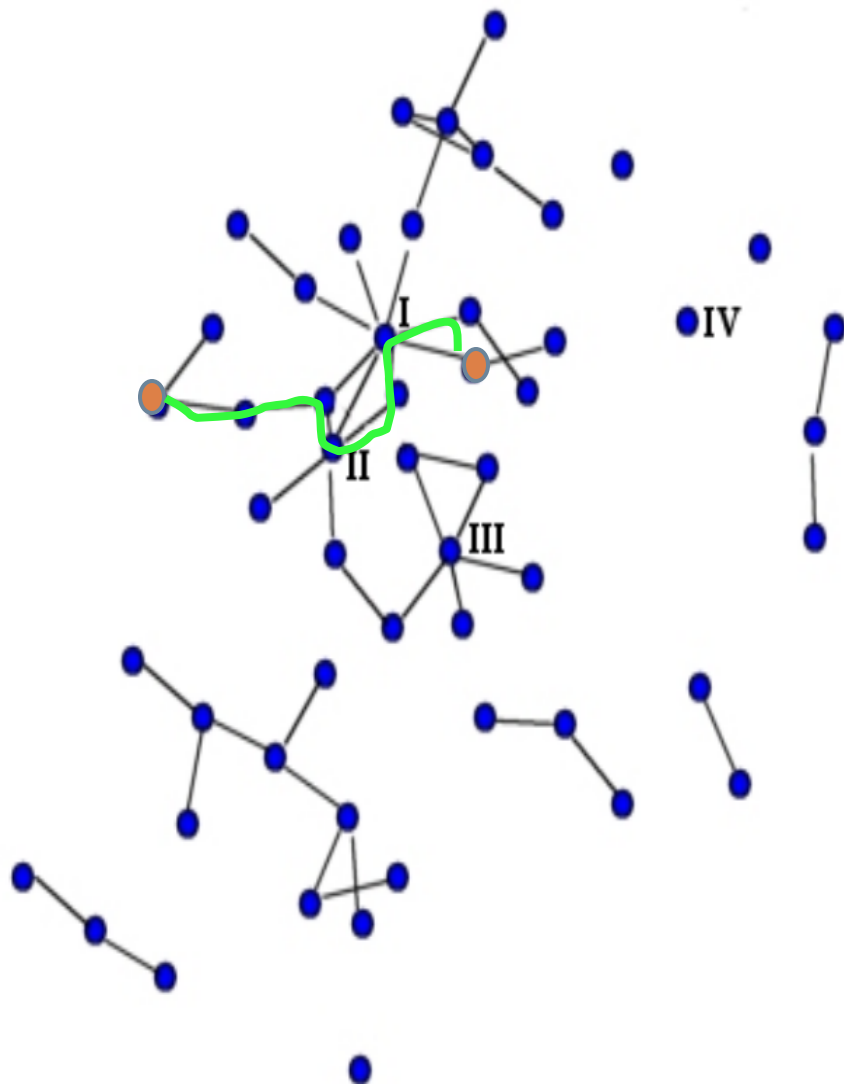
- How many possible paths are there between node  $N$  and node  $M$ , that do not repeat a node?

# What is the flow?

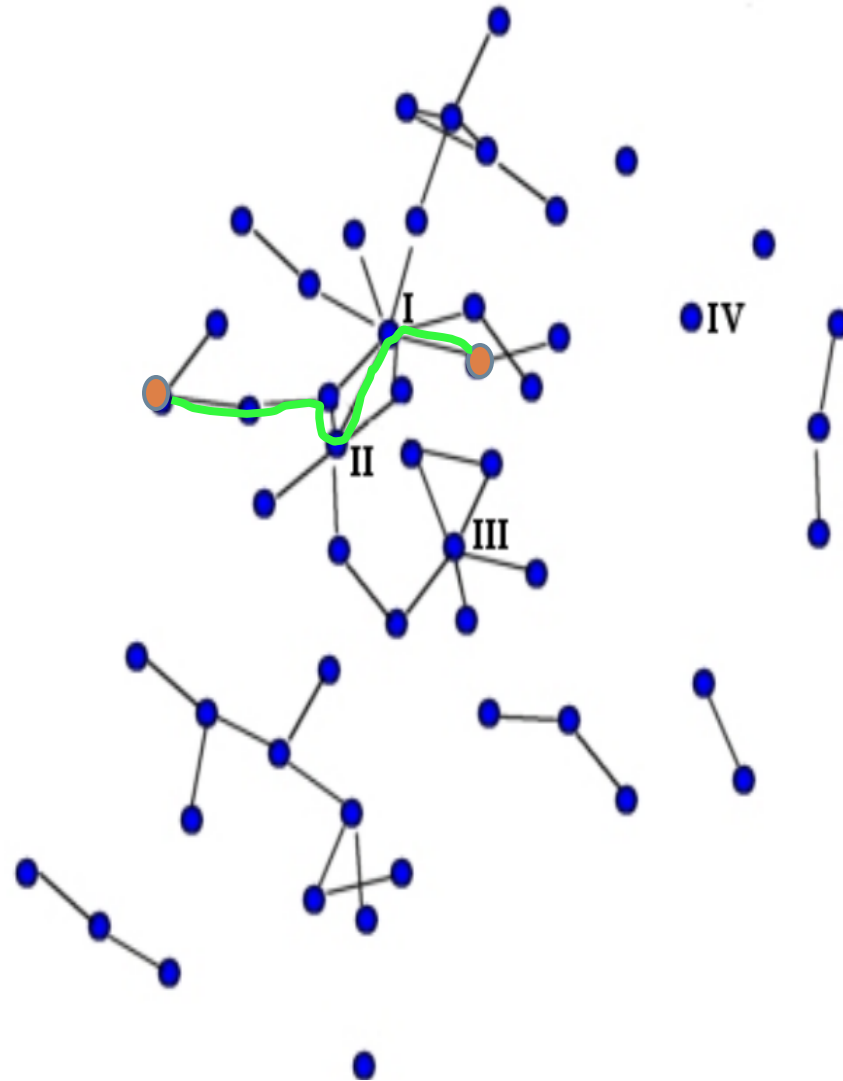




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# Flow

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- How many possible paths are there for an idea to go between people?



# Centrality

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- How important is a node within the graph?
- Which kids are the popular or influential kids?

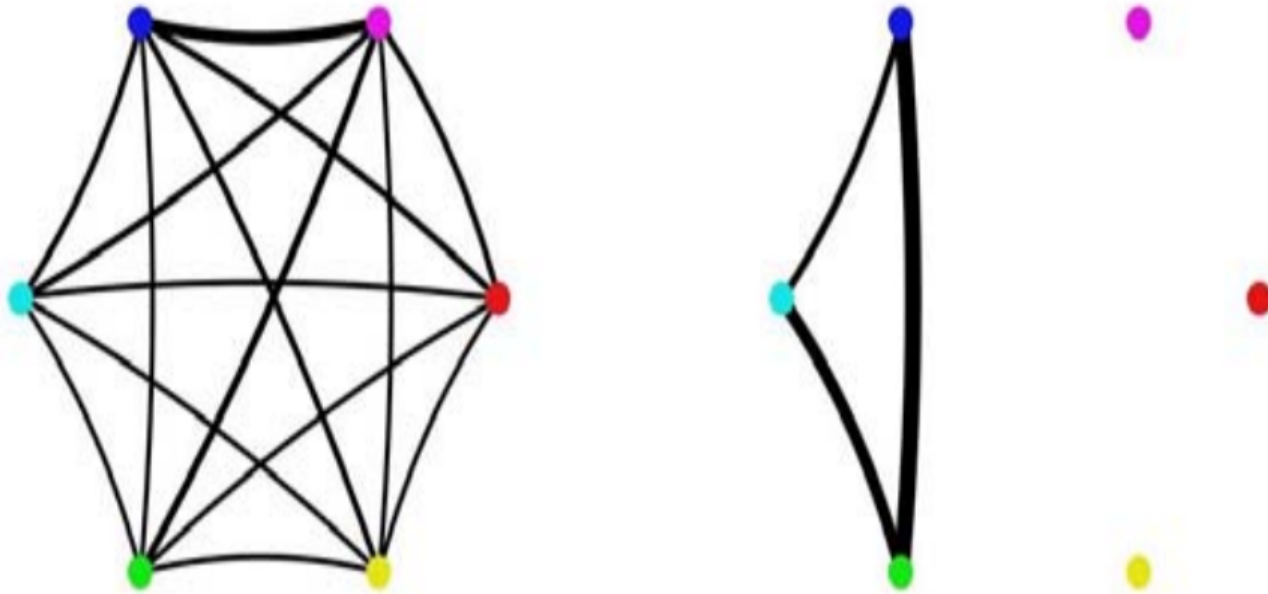
# Centrality

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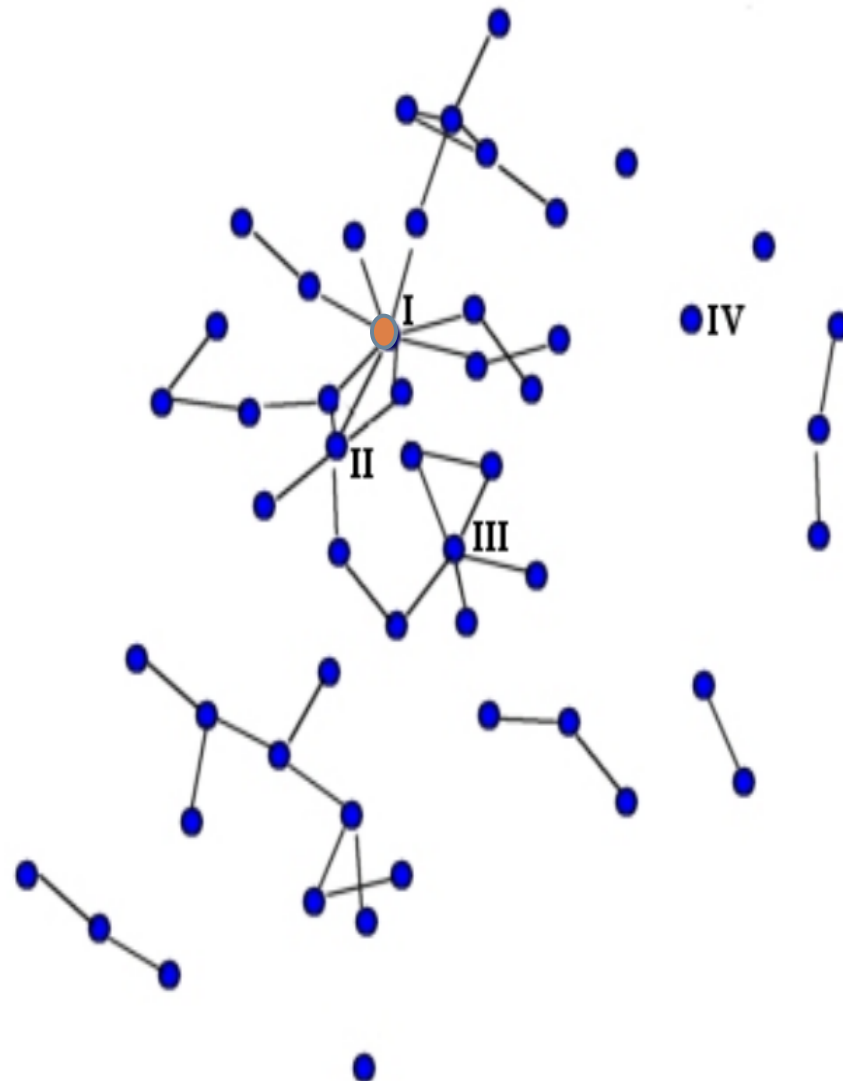
- Four common measures
  - ▣ Degree centrality
  - ▣ Closeness centrality
  - ▣ Betweenness centrality
  - ▣ Eigenvector centrality

# Nodal Degree

- Number of lines that connect to a node



# The node with the highest nodal degree



# Nodal Degree

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- Indegree: number of lines that come into a node
- Outdegree: number of lines that come out of a node

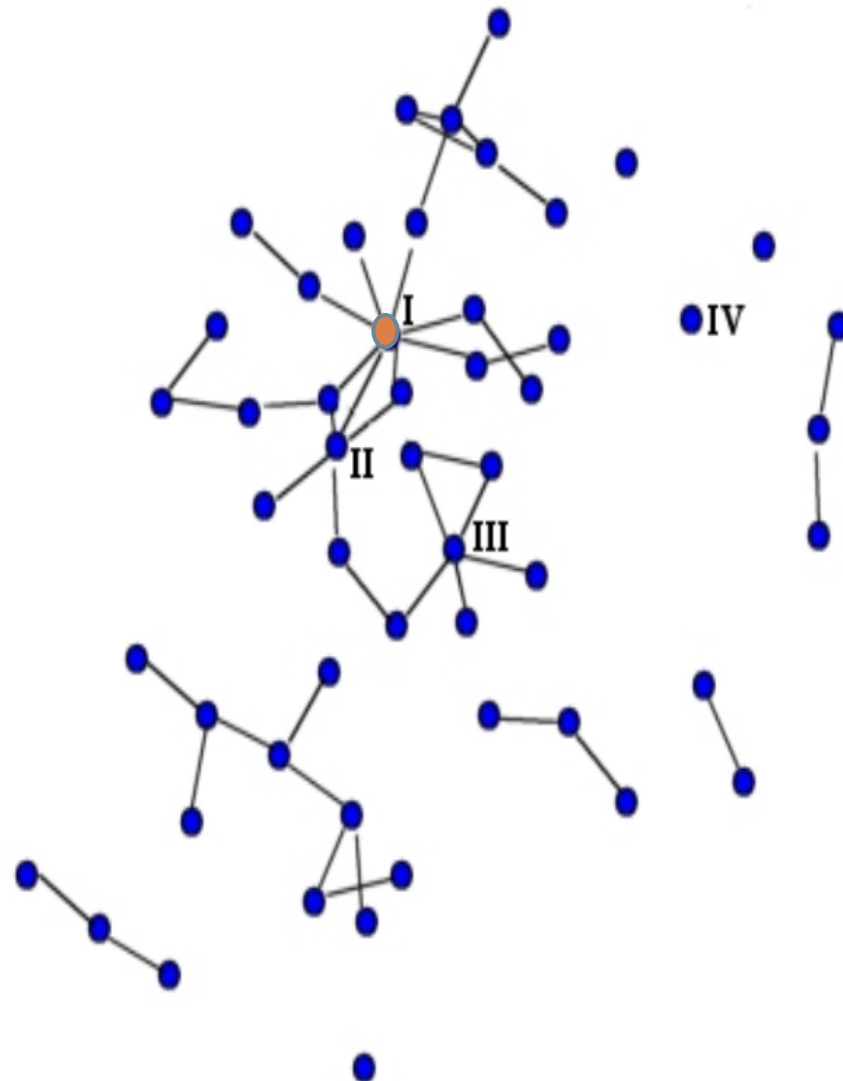
# Closeness

- A node N's closeness is defined as the sum of its distance to other nodes
- The most central node in terms of closeness is the node with the lowest value for this metric
- Note that strengths can be used as a distance measure for calculating closeness
  - ▣ Higher strength = closer nodes

# Betweenness

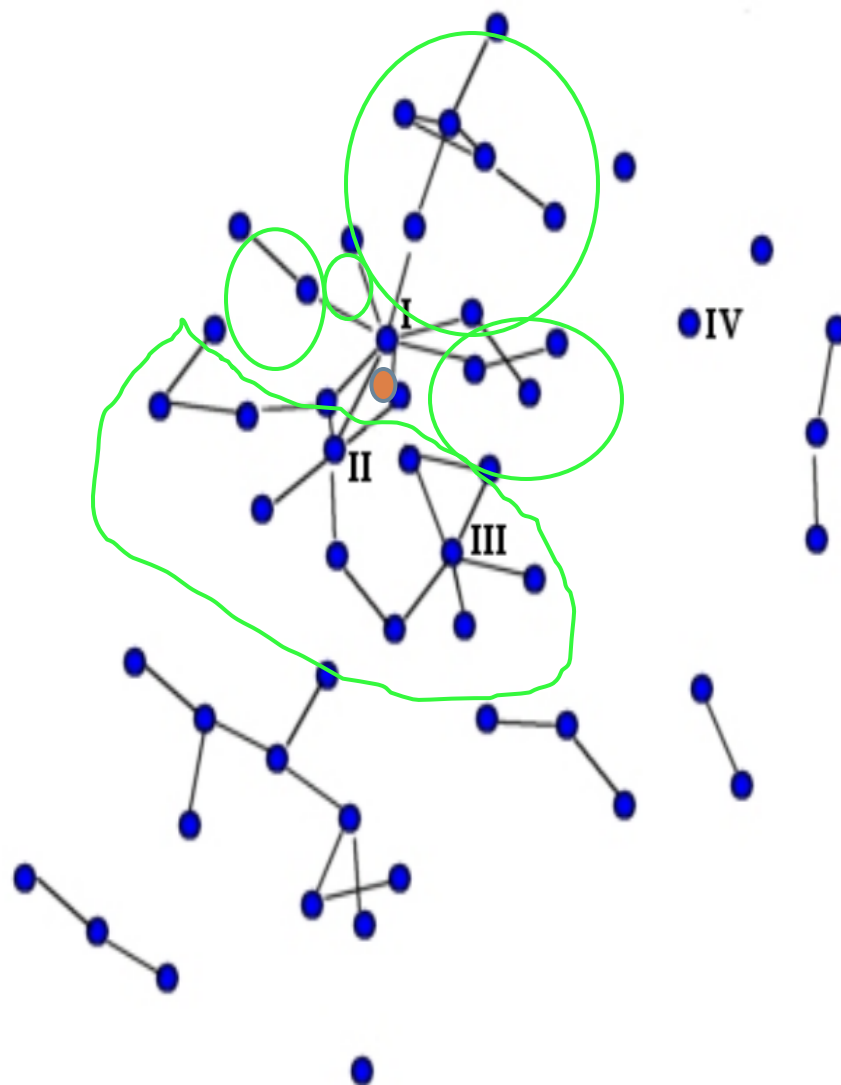
- Betweenness centrality for node  $N$  is computed as:
  - The percent of cases where
  - For each pair of nodes  $M$  and  $P$  (which are not  $N$ )
    - ▣ The shortest path from  $M$  to  $P$  passes through  $N$

# What is this node's betweenness

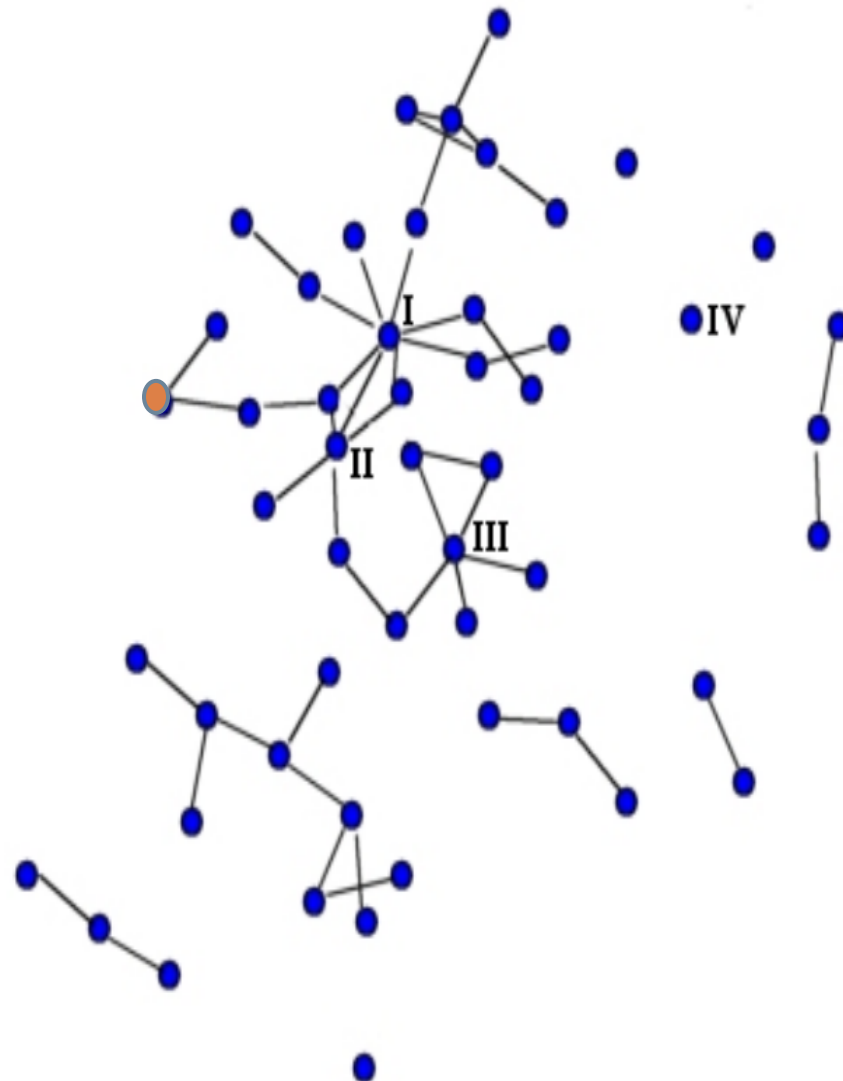




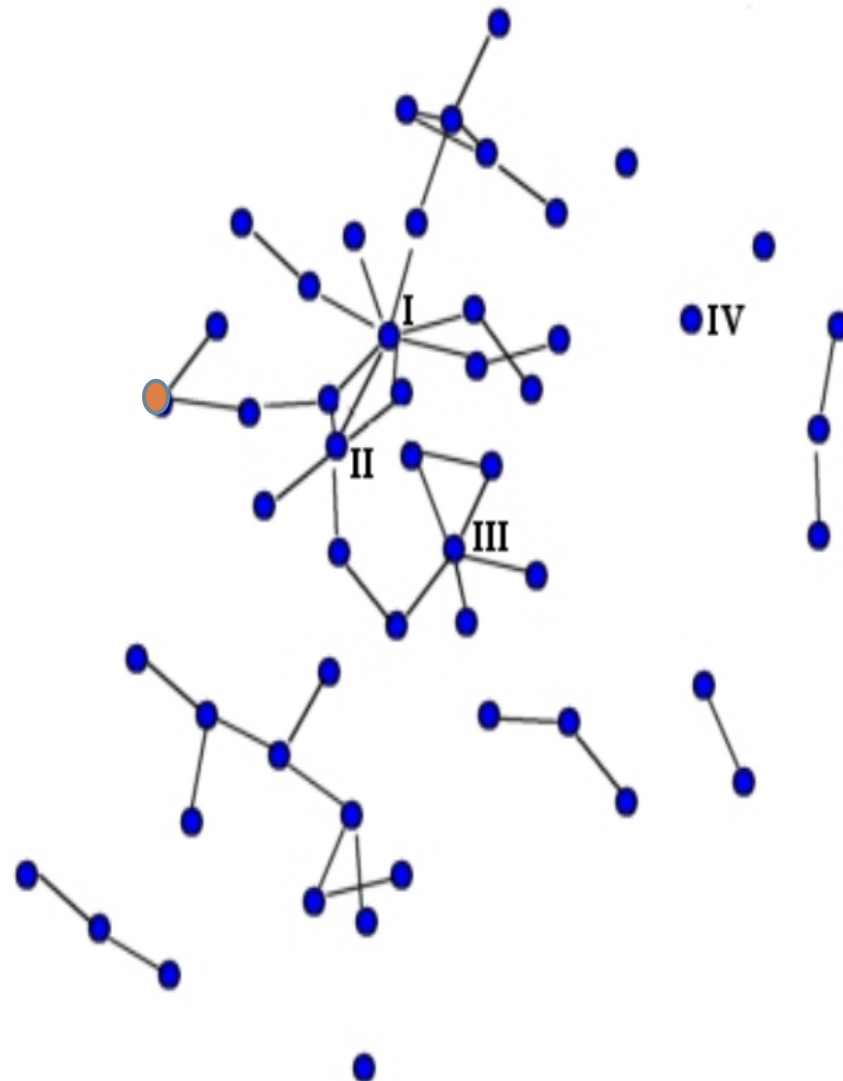
Betweenness is high;  
each group can only get to other groups through this point



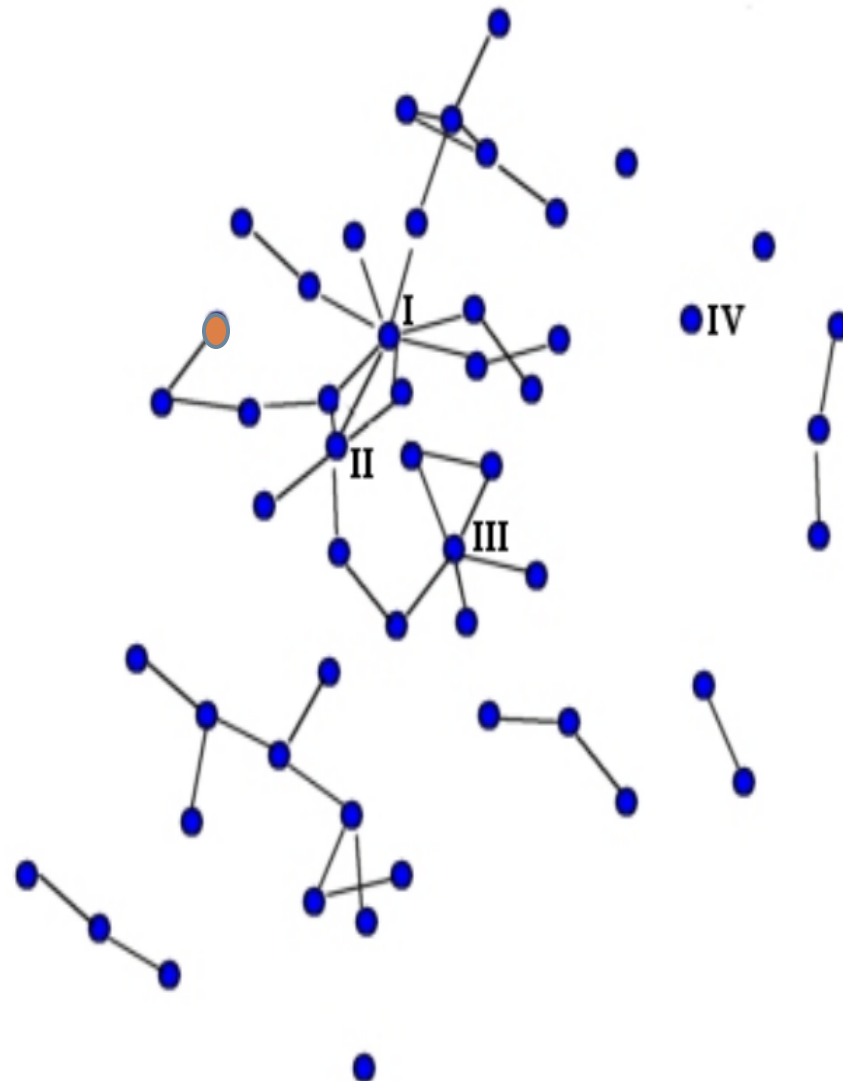
# What is this node's betweenness?



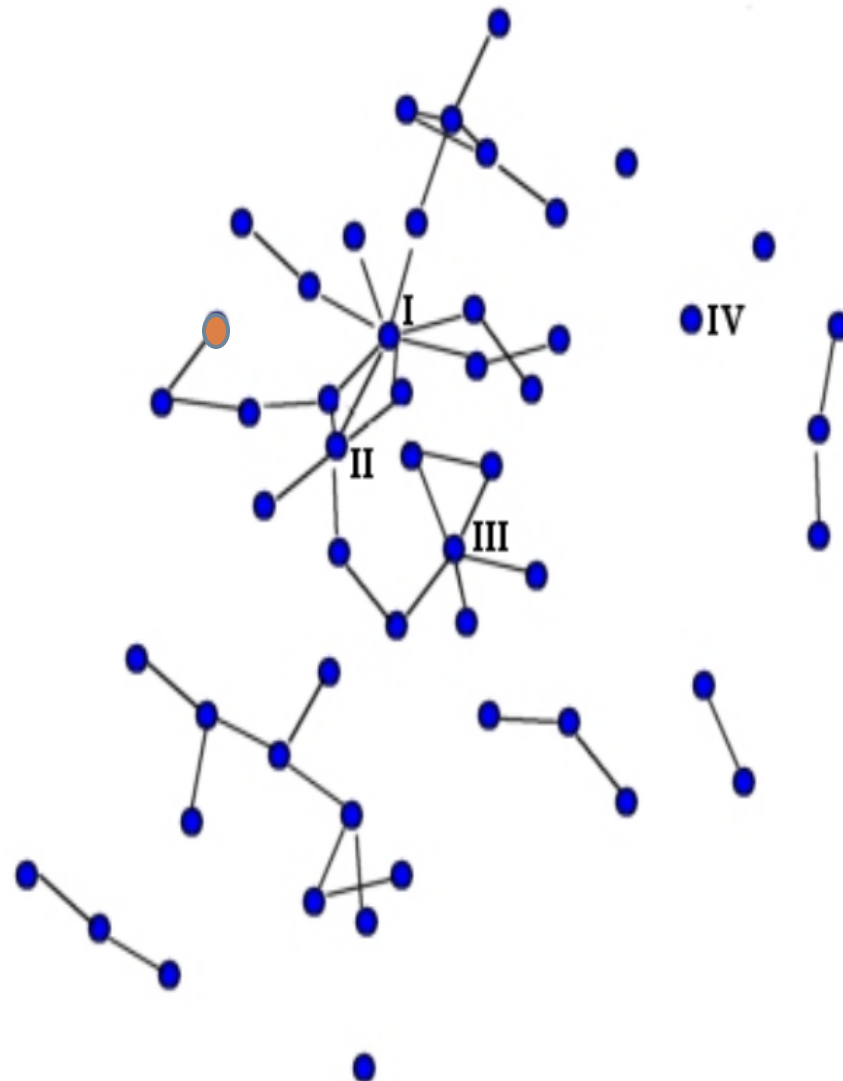
# Low, only one point connects through it



# What is this node's betweenness?



# Betweenness = 0



# Reciprocity

- What percentage of ties are bi-directional?
  - ▣ Can be computed as number of bi-directional ties over total number of connected pairs

# Eigenvector Centrality

- Complex math, but assigns centrality to nodes through recursive process where
- More and stronger connections are positive
- Connections to nodes with higher eigenvector centrality contribute more than connections to nodes with lower eigenvector centrality

# Eigenvector Centrality

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- A key part of the original PageRank in Google



# Lots of uses

- There are lots of uses for network analysis
- But particularly useful for studying collaboration
  - ▣ Group-based learning
  - ▣ Teacher collaboration
  - ▣ Networks of influence
    - Why do some educational interventions seem to be dominant in specific regions?

# Next lecture: Epistemic Networks

